## AP® CHEMISTRY 2006 SCORING GUIDELINES

## Question 1

- 1. Answer the following questions that relate to solubility of salts of lead and barium.
  - (a) A saturated solution is prepared by adding excess  $PbI_2(s)$  to distilled water to form 1.0 L of solution at  $25^{\circ}_{-}$ C. The concentration of  $Pb^{2+}(aq)$  in the saturated solution is found to be  $1.3 \times 10^{-3} M$ . The chemical equation for the dissolution of  $PbI_2(s)$  in water is shown below.

$$PbI_2(s) \rightleftharpoons Pb^{2+}(aq) + 2 I^{-}(aq)$$

(i) Write the equilibrium-constant expression for the equation.

$$K_{sp} = [Pb^{2+}][I^{-}]^{2}$$

One point is earned for the correct expression.

(ii) Calculate the molar concentration of  $I^-(aq)$  in the solution.

By stoichiometry, 
$$[I^-] = 2 \times [Pb^{2+}]$$
,  
thus  $[I^-] = 2 \times (1.3 \times 10^{-3}) = 2.6 \times 10^{-3} M$ 

One point is earned for the correct concentration.

(iii) Calculate the value of the equilibrium constant,  $K_{sp}$ .

$$K_{sp} = [Pb^{2+}][I^{-}]^{2} = (1.3 \times 10^{-3})(2.6 \times 10^{-3})^{2}$$
  
=  $8.8 \times 10^{-9}$ 

One point is earned for a value of  $K_{sp}$  that is consistent with the answers in parts (a)(i) and (a)(ii).

(b) A saturated solution is prepared by adding  $PbI_2(s)$  to distilled water to form 2.0 L of solution at 25°C. What are the molar concentrations of  $Pb^{2+}(aq)$  and  $I^{-}(aq)$  in the solution? Justify your answer.

The molar concentrations of  $Pb^{2+}(aq)$  and  $I^{-}(aq)$  would be the same as in the 1.0 L solution in part (a) (i.e.,  $1.3 \times 10^{-3}\,M$  and  $2.6 \times 10^{-3}\,M$ , respectively). The concentrations of solute particles in a saturated solution are a function of the constant,  $K_{sp}$ , which is independent of volume.

One point is earned for the concentrations (or stating they are the same as in the solution described in part (a)) and justification.

## AP® CHEMISTRY 2006 SCORING GUIDELINES

## Question 1 (continued)

(c) Solid NaI is added to a saturated solution of  $PbI_2$  at 25°C. Assuming that the volume of the solution does not change, does the molar concentration of  $Pb^{2+}(aq)$  in the solution increase, decrease, or remain the same? Justify your answer.

[Pb<sup>2+</sup>] will decrease.

The NaI(s) will dissolve, increasing [I<sup>-</sup>]; more I<sup>-</sup>(aq) then combines with Pb<sup>2+</sup>(aq) to precipitate PbI<sub>2</sub>(s) so that the ion product [Pb<sup>2+</sup>][I<sup>-</sup>]<sup>2</sup> will once again attain the value of  $8.8 \times 10^{-9}$  ( $K_{sp}$  at 25°C).

One point is earned for stating that [Pb<sup>2+</sup>] will decrease.

One point is earned for justification (can involve a Le Chatelier argument).

- (d) The value of  $K_{sp}$  for the salt BaCrO<sub>4</sub> is  $1.2 \times 10^{-10}$ . When a 500. mL sample of  $8.2 \times 10^{-6} M$  Ba(NO<sub>3</sub>)<sub>2</sub> is added to 500. mL of  $8.2 \times 10^{-6} M$  Na<sub>2</sub>CrO<sub>4</sub>, no precipitate is observed.
  - (i) Assuming that volumes are additive, calculate the molar concentrations of  $Ba^{2+}(aq)$  and  $CrO_4^{2-}(aq)$  in the 1.00 L of solution.

New volume = 500. mL + 500. mL = 1.000 L, therefore  $[Ba^{2+}]$  in 1.000 L is one-half its initial value:

$$[Ba^{2+}] = \frac{500 \text{ mL}}{1,000 \text{ mL}} \times (8.2 \times 10^{-6} M) = 4.1 \times 10^{-6} M$$

$$[\text{CrO}_4^{2-}] = \frac{500 \text{ mL}}{1,000 \text{ mL}} \times (8.2 \times 10^{-6} M) = 4.1 \times 10^{-6} M^{-1}$$

One point is earned for the correct concentration.

(ii) Use the molar concentrations of  $\mathrm{Ba^{2+}}(aq)$  ions and  $\mathrm{CrO_4^{2-}}(aq)$  ions as determined above to show why a precipitate does not form. You must include a calculation as part of your answer.

The product 
$$Q = [Ba^{2+}][CrO_4^{2-}]$$
  
=  $(4.1 \times 10^{-6} M)(4.1 \times 10^{-6} M)$   
=  $1.7 \times 10^{-11}$ 

Because  $Q=1.7\times 10^{-11}<1.2\times 10^{-10}=K_{sp}$  , no precipitate forms.

One point is earned for calculating a value of Q that is consistent with the concentration values in part (d)(i).

One point is earned for using Q to explain why no precipitate forms.